Effects of Charging and Electric Field on Graphene Oxide

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ABSTRACT: We present a first-principles study of various effects of charging and electric field on the oxidation/deoxidation of graphene oxide consisting of only epoxy groups. We first determined the proper basis set, which hinders the spurious spilling of electrons of graphene oxide when negatively charged or exerted by perpendicular electric field, and treated with periodic boundary conditions. We then showed that the electric field perpendicularly applied to graphene surface provide side-specific functionalization. We found that the bonds between oxygen and graphene are weakened under applied electric field. For specific values of excess charge or electric field, an oxygen atom that is normally adsorbed to the bridge site in equilibrium moves to the top site. By directly charging and/or by applying electric field, one can monitor this migration as well as desorption of the oxygen adatom. In spite of the negative formation energy, an energy barrier prevents individually adsorbed oxygen atoms from forming oxygen molecules. This energy barrier is dramatically weakened upon negative charging or exertion of an electric field. Our results explain why the reduction of graphene oxide can be facilitated by these external effects.

INTRODUCTION

Despite a great deal of experimental and theoretical research carried out recently,1−16 the interaction of oxygen with graphene and the resulting oxidation/deoxidation reactions are not fully understood yet. Following the first synthesis of single-layer graphene,17 graphene oxide (GOX) has been the focus of interest because it provided a potential method for the production of large-scale graphene sheets through the reduction of oxidized multilayer graphenes.1,2 Active research to date has concluded that the oxidation and reduction of graphene are, in fact, rather complex and comprise the interplay of various molecules and atoms, such as O, O₂, CO₂, OH, H, and H₂O. GOX by itself can be obtained through oxidative exfoliation of graphite, which can be visualized as an individual sheet of graphene decorated with epoxy (C−O−C) and hydroxyl (C−OH) groups on both sides and edges. Recently, it has been shown that multilayer GOX produced by oxidizing epitaxial graphene is a metastable material, whose structure and chemistry evolve at room temperature within approximately 1 month.14 While maximum oxygen coverage of graphene can be as high as 50%, it is reduced to 38% in equilibrium.14 Nonetheless, domains of graphene monoxide with C/O ratio of unity are attained by the oxidation of both sides.9 It is now well-established that the properties of graphene emerge from its linearly crossing bands at the Fermi level, which undergo dramatic changes upon oxidation,16,20−22 even if one does not know yet how the oxidation takes place and what the character of oxygen coverage is. Introducing a band gap, which varies with oxygen coverage, and hence changing semimetallic graphene into a semiconductor, has been an active field of study in graphene-based nanoelectronics.16,22

Intriguing conclusions obtained from recent studies attracted further interest on the seemingly reversible oxidation and deoxidation processes of graphene. Wei et al.20 showed that one can write on oxidized graphene by the heated tip of a scanning tunneling microscope (STM), whereby the light-reflecting (semiconducting) places on the oxidized graphene turn to be dark (or become metallic) after they are traced by the tip. This interesting result leading to thermochemical nanolithography is interpreted as the reduction (or deoxidation) of oxidized graphene. In another work by Ekiz et al.,22 it is reported that the oxidized surface of graphene can be changed reversibly
between dark and light spots with applied lateral electric field, which in turn changes the surface between (+) and (−) polarity depending on the direction of the electric field. Here they also attributed dark (light) spots to metallic (semiconducting) regions on the surface. Additionally, the extend of reduction can be also controlled by the applied electric field to tune the band gap.\textsuperscript{22} Deoxidized spots can also be achieved underneath the tip of an STM under specific bias.\textsuperscript{22} These results pointout the crucial feature: namely, modification of the properties of graphene by the controlled and reversible reduction/oxidation of GOX, which is realized by charging it positively or negatively or by applying an electric field to it perpendicularly or laterally.

The formation energy related to the oxidation of graphene is negative, and hence graphene cannot be oxidized through oxygen molecules.\textsuperscript{16,16} Actually, O\textsubscript{2} is physisorbed to bare graphene surface with a very weak binding energy of 58 meV calculated without van der Waals correction, but it rises to 115 meV when the van der Waals correction is included. Only at defect sites like holes and vacancies can O\textsubscript{2} dissociate and its constituent oxygen atoms become adsorbed to carbon atoms having lower coordination numbers.\textsuperscript{19} In contrast to O\textsubscript{2}, the bonding of free oxygen to graphene is rather strong and varies between 2.43 and 3.20 eV depending on the coverage.\textsuperscript{16} The crucial questions to be addressed are how oxygen atoms can remain strongly bound to graphene despite their negative formation energy and why bound oxygen atoms are prevented from desorption through the formation of oxygen molecules. Recent studies have provided the energy barrier for diffusion of adsorbed O on graphene and for desorption of O through the formation of O\textsubscript{2} and CO\textsubscript{2}.\textsuperscript{10,16}

The objective of this paper is to provide a better understanding of recent experimental studies reporting that external agents cause rapid reduction or, conversely, rapid oxidation of graphene oxide. In this context, we investigated the external agents, such as positive or negative charging and electric field applied perpendicular to the graphene layer, that were involved in recent experimental studies related to reduction/oxidation of graphene oxide. Here we will focus our attention only on oxygen atoms adsorbed to graphene and do not consider other impurities, such as hydroxyl groups and hydrogen adatoms. We performed the calculations for charged graphene oxide by adding a desired amount of excess electrons (for the case of negative charging) or by removing electrons (for the case of positive charging), and both cases are treated with periodic boundary conditions (PBC). We examined also the behavior of oxidized graphene under a perpendicular electric field. In addition, this paper presents a comprehensive evaluation of the plane wave (PW) and local (atomic orbital, AO) basis sets in first-principles calculations of charged systems using PBC.

### THEORETICAL STUDIES OF CHARGED SYSTEMS

Recently, the theoretical investigations of charged nanosystems have been an active field of study. Poloni et al.\textsuperscript{24} studied the interplay between charge doping and intermolecular distance in the polymerization of C\textsubscript{60} fullerene chains using AO calculations. They show that the polymerization depends on both the center-to-center distance of fullerenes and the negative doping of the system. In particular, they observed that up to a doping of four electrons per two molecules, the energy barrier, which is related to the formation energy of covalent bonds between fullerenes, progressively decreases. PW calculations using PWSCF code by Attaccalite et al.\textsuperscript{25} proposed a new way of tuning the electron–phonon coupling (EPC) in graphene by changing the deformation potential with electron/ hole doping. The doping is simulated by changing the number of electrons in the unit cell. They show that the EPC for highest optical branch at the K-point in BZ acquires a strong dependency on the doping level due to electron–electron correlation. Density functional tight binding method\textsuperscript{26,27} (DFTB\textsuperscript{+}) has also been used to explore the effective failure limit of graphene with respect to induced anionic charge produced by electron beam or electric current.\textsuperscript{28} It was predicted that graphene flakes are resistant to high level of charging, posing no problem in the operation of graphene-based electronic devices, but the localized regions were shown to be transformable from sp\textsuperscript{2}-bonded into sp\textsuperscript{3}-bonded material before the failure limit. Using DMO\textsuperscript{3} code,\textsuperscript{29} Ao et al.\textsuperscript{30} demonstrated that the applied electric field can significantly facilitate the binding of hydrogen molecules on N-doped graphene through dissociative adsorption and diffusion on graphene surface. By removing the electric field, stored hydrogens on graphene can be released efficiently under ambient conditions when the hydrogen concentration is higher than 0.5 wt %, which indicates that N-doped graphene can be used as a hydrogen storage material with a storage capacity of 6.73 wt %. Assuming that varying the number of electrons in an adatom–graphene system can be used to simulate the effects of gate voltage, Chan et al.\textsuperscript{31} demonstrate the ionization of Li and Co adatoms by doping. The ionization is accompanied by a sharp change in the electrostatic potential of the adatom. These results were consistent with recent STM experiments for Co on graphene.\textsuperscript{32} The exfoliation of graphite under static positive charge is demonstrated by PW effects of the charging and electric field are obtained from AO calculations using SIESTA.\textsuperscript{40}

A plane-wave basis set with kinetic energy cutoff of 500 eV is used in PW calculations.\textsuperscript{39} Atomic positions and lattice constants are optimized by the conjugate gradient method, where the total energy and atomic forces are minimized. The convergence for energy is chosen as 10\textsuperscript{−5} eV between two steps. An oxygen adatom adsorbed to one side of graphene breaks inversion symmetry, and a net electric-dipole moment is generated perpendicular to the graphene surface. Dipole corrections\textsuperscript{46} are applied in order to remove spurious dipole interactions between periodic images for the neutral calculations.

In AO calculations,\textsuperscript{40} the eigenstates of the Kohn–Sham Hamiltonian are expressed as linear combinations of numerical atomic orbitals. A 200 Ryd mesh cutoff is chosen and the self-consistent calculations are performed with a mixing rate of 0.1. Core electrons are replaced by norm-conserving, nonlocal Troullier–Martins pseudopotentials.\textsuperscript{41} The convergence criterion for the density matrix is taken as 10\textsuperscript{−4}.

### METHODOLOGY

We carried out spin-polarized and spin-unpolarized calculations within density functional theory (DFT) using projector-augmented wave potentials.\textsuperscript{37} The exchange–correlation potential is approximated by generalized gradient approximation using Perdew, Burke and Ernzerhof (PBE) functional.\textsuperscript{38} Initially, we used two different basis sets, namely, plane waves (PW) and local basis (AO) sets for reasons explained below, which are applied by using first-principles simulation packages VASP\textsuperscript{59} and SIESTA\textsuperscript{40} respectively. Based on the results derived from the test calculations, all of our conclusions concerning the effect of the charging and electric field are obtained from AO calculations using SIESTA.\textsuperscript{40}
calculations. In another PW study carried out with VASP code, Suarez et al. analyzed the diffusion of oxygen adatoms on graphene and its dependence on the carrier density controlled by a gate voltage. The energy barrier, which is related to the diffusivity of oxygen on graphene, was predicted to be strongly dependent on the carrier density.

Normally, PBC realized by repeating charged supercells has a divergent electric potential energy and has drawbacks and limitations, which have been the subject matter of several studies in the past. Additional background charge of opposite polarity has been added to neutralize the excess charge and hence to achieve the convergence of electronic potential. Even with this correction, calculations carried out with PBC and plane wave basis sets became strongly dependent on certain parameters of calculations, such as vacuum spacing $s$ between consecutive slabs.

**Comparison of Methods Used in the Calculation of Charged Graphene.** Before we start to investigate the effects of charging on oxygen-adsorbed graphene, we first examine the limitations of the PBC method, where two-dimensional graphene layers separated by large spacing $s$ are repeated periodically along the $z$-direction. We carried out first-principles PW calculations as well as AO calculations using linear combinations of numerical atomic orbitals, and we investigated the effect of charging on the graphene layer. Throughout the paper, $Q > 0$ (or surface charge density $\sigma = Q/A$ in coulombs per square meter, $A$ being the area of the cell) indicates positive charging, or the number of depleted electrons per cell; $Q < 0$ indicates negative charging, or the number of excess electrons per cell; and $Q = 0$ is the neutral cell. The (super)cell is made up of $(n \times n)$ primitive unit cells of graphene; each supercell comprises $2n^2$ carbon atoms and $8n^3$ valence electrons. We assume that graphene planes, which are repeating periodically along the $z$-axis, are parallel to the $xy$-plane. In Figure 1a–c we present electronic band structures of graphene calculated by PW and AO for $Q = 0.2$ electron/cell ($\sigma = 0.61$ C/m$^2$), $Q = 0$ electron/cell, and $Q = 0.2$ electron/cell ($\sigma = 0.61$ C/m$^2$) for the primitive cell ($n = 1$). Further details about the changes in the band structure of graphene upon charging have been discussed in our recent studies. In the case of $Q = +0.2$ ($\pi = 0.61$ C/m$^2$), the Fermi level shifts down or the Dirac point rises for both PW and AO calculations. Accordingly, semimetallic graphene turns into a hole-doped metallic system.

For the neutral case ($Q = 0$), band structures calculated using PW and AO are similar. The work function, the minimum energy that must be given to an electron to release it from the plane of graphene, is the difference between the reference vacuum energy and Fermi level. The value of work function extracted from Figure 1b is 4.26 eV, and this is in good agreement with an earlier study. Brieflly, the results calculated using PW and AO are similar. Minute differences originate from different pseudopotentials used in calculations. Moreover, perfect convergences of different basis sets can be achieved only by using very large cutoff values.

As for the case of negative charging with $Q = -0.2$ e/cell ($\bar{\sigma} = -0.61$ C/m$^2$), the Fermi level shifts up significantly in AO results. In the PW results, the Fermi level shifts up only slightly and then is pinned by the free electron-like parabolic bands touching to the Fermi level; thereafter the position of the Fermi level is practically unaltered with increasing negative charging as shown in Figure 1c. The dramatic difference for the case of $Q < 0$ between PW and AO results can be understood through the plane-averaged electronic potential along the $z$-direction, that is, $\overline{V(z)}$ as described schematically in Figure 1d. In the actual case, $\overline{V(z)}$ passes through a maximum near the surface and goes to $-\infty$ as $z \rightarrow \pm \infty$ at both sides of one single graphene layer, which is charged with $Q < 0$. Then the electrons in the graphene can spill to vacuum only if they tunnel through tunneling across a wide triangular barrier. The width of the barrier, $w$, decreases with increasing negative charging. Accordingly, the tunneling current would be negligibly low and excess electrons would practically be trapped in graphene if the value of $|Q|$ is not very high. However, when treated within

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**Figure 1.** (a–c) Energy band structures of graphene calculated for (a) $Q = +0.2$ e/primitive unit cell ($\sigma = 0.61$ C/m$^2$), (b) $Q = 0$ e/primitive unit cell, and (c) $Q = -0.2$ e/primitive unit cell ($\sigma = -0.61$ C/m$^2$). Left-hand panels are calculated with PW basis set using VASP code; right-hand panels are calculated with AO basis set using SIESTA code. (d) Schematic description of plane-averaged potential of negatively charged graphene, $\overline{V(z)}$, dipping at the center of vacuum spacing and forming a quantum well-like structure. The vacuum spacing between two adjacent graphene planes is denoted by $s$. The triangular potential barrier and its width are $\Phi_B$ and $w$, respectively. The quantum well confining electrons, which are spilled from charged graphene of PW calculations, is illustrated by blue lines; the well without bound electrons, shown by red lines, corresponds to AO calculations. For one single graphene layer corresponding to the “actual case”, $\overline{V(z \rightarrow \pm \infty)} \rightarrow -\infty$ for $s \rightarrow \infty$. (e) Plane-averaged (linear) charge density, $\lambda(z)$, obtained from PW calculations for $Q = -0.2$ e/cell ($\sigma = -0.61$ C/m$^2$) and $s = 20$ Å. $\lambda(z)$ in full $y$-axis range is shown in the inset. Here “cell” indicates the primitive unit cell, and $s = 20$ Å.
PBC, $V(z)$ of periodically repeating graphene layers with a vacuum spacing $s$ between them can make a dip reminiscent of a quantum well at the center of the spacing as shown in Figure 1d. Under these circumstances, Kohn–Sham Hamiltonian using PW can acquire solutions in this quantum well, which are localized along the z-direction but are free-electron-like in the $x$-$y$-plane parallel to graphene. These states form the parabolic bands ($k_x, k_y$) plane as shown in Figure 1c. If the quantum well dips below the Fermi level with increasing $s$ or $Q$, excess electrons in graphene start to be accommodated in these 2D free-electron-like bands. This ends up with the spilling of excess electrons in graphene start to be accommodated in these 2D free-electron-like bands. This ends up with the spilling of excess electrons into the vacuum region. In Figure 1e we present the plane-averaged charge density, $\lambda(z)$, calculated within PW. By integrating $\lambda(z)$ along the z-direction, it is concluded that graphene can keep only $-0.09$ e/cell ($\bar{\sigma} = -0.28 \text{ C/m}^2$) out of $-0.2$ e/cell ($\bar{\sigma} = -0.61 \text{ C/m}^2$) excess electrons. The remaining $-0.11$ e/cell ($\bar{\sigma} = -0.33 \text{ C/m}^2$) are spilled out into the vacuum, namely, to the region between two adjacent graphene planes. Clearly, the spilling of excess electrons, which can be normally trapped in graphene, is an artifact of PBC. The amount of excess electrons spilled to the vacuum spacing increases with increasing $s$ and increasing negative charging. While wide $s$ is not convenient because of excessive charge spilling, small $s$ may prevent excess electrons from spilling into the vacuum at very low negative charging and can yield reasonable solutions as long as the coupling of the adjacent layers is negligible. However, the charge spilling can set in when the negative charging exceeds a threshold value corresponding to the given $s$.

The dependency of electronic structure and hence the band gap opening on $s$ in PW calculations of silicene (graphene-like Si) under perpendicular electric field has been also reported recently. The perpendicular electric field breaks the mirror symmetry of $V(z)$ and gives rise to a sawtooth-like variation. At high $E$ and large $s$, electrons of silicene spilling to low-potential site result in a situation above for $Q < 0$.

In AO calculations, the spurious quantum well-like structure at the middle of vacuum spacing between graphene layers in PBC is devoid of basis set, and hence cannot support the bound electronic states, which shall be localized along z-direction, but free-electron-like in the $x$-$y$-plane, since the local atomic orbitals are placed only at the atomic sites. This is why $V(z)$ calculated by AO does not accommodate excess electrons in its minimum between graphene layers, even if it is further lowered below the Fermi level with increasing $s$. The behavior of $V(z)$ at the proximity of the surface is similar to the actual case, where $s \to \infty$. Accordingly, excess negative charge is prevented from spilling into the spacing between adjacent graphene layers, and hence remains in graphene, as in the actual case consisting of one single graphene charged by $Q < 0$.

In contrast to the above shortcomings arising in PW method in treating the negative charging $Q < 0$ of graphene using PBC, results obtained by AO and PW agree for $Q \geq 0$. For $Q < 0$, $V(z)$ passes through a maximum at the center of $s$ between graphene layers. Accordingly, a method using PBC and plane-wave basis set is not affected significantly by the size of vacuum spacing $s$ if $Q \geq 0$, as pointed out in ref 42.

Figure 2. (a) Description of NEB trajectories going from the bridge site to the adjacent bridge site through the top site. Oxygen adatom and carbon atoms of graphene are indicated by a large red sphere and small brown spheres, respectively. (b) Variation of total energies $E_T$, calculated by PW for different values of charging $Q$ at a fixed vacuum spacing $s = 20 \text{ Å}$. (c) Variation of $E_T$ calculated by PW for different values of $s$ at a fixed charging $Q = -1.0$ e/cell ($\bar{\sigma} = -0.12 \text{ C/m}^2$). Panels d and e are the same as panels b and c but are calculated by AO. The calculated total energies at the B-site are set to zero for all cases. Calculations are performed for a single oxygen atom adsorbed to each (5 $\times$ 5) (super)cell of graphene.
Comparison of Methods Used in the Calculation of Oxygen Adsorbed to Charged Graphene. Having discussed the capacity of plane-wave and local basis sets in representing charged graphene using PBC, we next explore the similar situation for oxygen adatoms. When neutral, a single oxygen is adsorbed at the bridge site of graphene, above the center of the C–C bonds of honeycomb structure. Both PW and AO calculations yield that the bridge site (B-site) is energetically the most favorable adsorption site; the top sites (T-sites, on top of carbon atoms) are not favorable. PW calculations predicted the binding energies of a single oxygen at the B-site as 2.35, 2.40, 2.43, and 2.43 eV for (2 × 2), (3 × 3), (4 × 4), and (5 × 5) supercells of graphene, respectively. The binding energy is practically unaltered for supercells larger than (5 × 5). Using AO, we found that the binding energy of oxygen on (5 × 5) graphene supercell is 2.34 eV. As calculated from the Bader analysis, the charge of 0.78 e is transferred from graphene to oxygen atom adsorbed to graphene. The spurious dependence of the energy on the spacing between periodically repeating graphenes, s, is examined by performing NEB (nudged elastic band) calculations of adsorbed oxygen between two adjacent B-site positions through the T-site position described in Figure 2a. Results obtained from PW and AO calculations using (5 × 5) supercells are presented in Figure 2b–e. According to PW results obtained for s = 20 Å in Figure 2b, the energy difference between the T-site and B-site, $\Delta E$, increases with increasing positive charging ($Q > 0$) but decreases with increasing negative charging ($Q < 0$). For example, $\Delta E > 0.8$ eV for $Q = +0.5$ e/atom ($= +0.5/50$ C/m$^2$ atom or $\bar{\sigma} = +0.06$ C/m$^2$), while it is lowered to $\Delta E = 0.1$ eV for $Q = -1.0$ e/atom ($\bar{\sigma} = -0.12$ C/m$^2$). Incidentally, these results are similar to those obtained by Suarez et al. using PW.

One obtains essentially similar results from AO calculations in Figure 2d. However, $\Delta E$ calculated for $Q = -1.0$ e/atom ($\bar{\sigma} = -0.12$ C/m$^2$) by PW displays a strong dependence on s in Figure 2c, such that $\Delta E \sim 0.1$ eV calculated for s = 20 Å increases to $\Delta E = 0.32$ eV when the spacing between periodically repeating graphenes is increased to s = 50 Å. The situation with AO results is rather different, as outlined in Figure 2e: Practically, $\Delta E$ is not affected by the variation of s. This is due to the fact that the spilling of excess electrons into the spacing between graphene layers is hindered in AO calculations.

In concluding this section, we note the following: (i) The excess charge remaining (or trapped) in graphene predicted by AO calculations is physical for the actual case involving only one single graphene layer as discussed above. (ii) PW calculations correctly predict the charge spilling into the spurious quantum well-like structure in the vacuum region forming for large s as a result of the artifact of PBC. The artifact of PBC sets a limit to the amount of negative charging that can be treated by PW for any given width of the vacuum region. Hence, the PW calculations for negatively charged systems should not be used with s larger than the value where vacuum charging occurs. If the quantity of interest converges before this problem happens, the use of plane-wave codes does not introduce a spurious error as long as the coupling between two layers is negligible. However, since the vacuum charging also increases with increasing negative charging, caution has to be exercised in using small s values, whereby the couplings between adjacent graphene layers can affect the electronic potential near the graphene surface and cause deviations from the actual case. (iii) The spilling of electrons does not occur in AO calculations even if PBC is used, since local basis orbitals at carbon sites fail to represent states, which can be bound to the quantum well-like potential at the middle of the vacuum spacing. This artifact of AO calculations turns out to be an advantage, which properly cancels out the artifact of PBC. (iv) As described in Figure 1d, near the surface region the electronic potential of one single graphene layer trapping the excess charge in the actual case is close to that obtained by AO calculations using PBC, if the vacuum spacing between adjacent layers hinders the coupling between local basis set at carbon atoms of graphene. Since exponentially decaying atomic orbitals have most of their charge near the surface region, the results obtained from AO calculations for graphene are expected to be very close to the results of the actual case. (v) The above analysis can also be extended to graphene exerted by an electric field perpendicular to it, since a sawtooth-like electronic potential is formed and the excess electrons are spilled to the lower-lying side of electronic potential.

On the basis of the above analysis, we conclude that, in the calculations using PBC and localized atomic orbitals (AO), the spilling of excess electrons into the vacuum region between graphene layers is hindered. Accordingly, results obtained from AO calculations become independent of the vacuum spacing s and hence are close to those of the actual case. For these reasons, we carry out AO calculations to reveal the effect of charging and external electric field in the rest of the paper, and hence, all of our conclusions regarding the effect of charging and electric field on reduction/oxidation process are obtained by AO calculations using PBC.

## EFFECTS OF ELECTRIC FIELD AND CHARGING ON A SINGLE OXYGEN ADATOM

The effects of applied electric field and charging are interrelated. Upon the adsorption of oxygen atom, 0.78 electron is transferred from carbon atoms to oxygen in the neutral case. The electric field applied perpendicularly to the graphene, $E$, which is specified as positive if it is along z-direction (or it is pointing toward oxygen adatom). This electric field induces electronic charge transfer from the adsorbed oxygen to graphene or vice versa if its direction is reversed. Electric field-induced charge transfer modifies the charge distribution and hence affects the physical and chemical properties. Results obtained from this section will enlighten recent experimental studies performed for similar systems.

Interesting effects of electric field on oxygen-adsorbed graphene are summarized in Figure 3. The binding energy of the oxygen adatom increases with applied negative electric field, which is perpendicular to the surface and pointing in the direction opposite to oxygen. The height h of oxygen adatom from the graphene plane also increases, even if one expects the opposite trend. This paradoxical situation originates from the definition of the binding energy, $E_b$, of oxygen adsorbed to graphene, which is given by $E_b = E_f[O] + E_f[O + graphene, E] - E_f[O + graphene, E]$, in terms of the total energies of single neutral oxygen atom $E_f[O]$, of bare graphene under $E$, $E_f[O + graphene, E]$, and of single oxygen adsorbed to graphene under applied $E$, $E_f[O + graphene, E]$, all calculated by use of a $(S \times S)$ supercell. According to this definition, increasing $E_b$ does not mean that the bond between oxygen and graphene has become stronger. In fact, that $h$ increases with increasing negative $E$ implies the opposite situation.

Before we explain this paradoxical situation, we first consider charge rearrangements caused by $E$. Induced charge transfer...
depends on the direction of $\vec{E}$. In Figure 4 we present the effects of applied perpendicular electric field on the charge distribution and potential energy $\bar{V}(z)$. An electric field $\vec{E} = -1.0$ V/Å transfers electrons from the bottom side to the upper side of the graphene and also causes further transfer of carbon electrons to oxygen adatom as shown in Figure 4b. At the end, the total energy of the whole system increases. This effect creates an interesting situation also for the bare graphene by breaking the projection symmetry between its two sides. The direction of electron transfer is reversed when the direction of the applied electric field is reversed. Accordingly, one can monitor various properties of bare graphene, in particular its chemical activity, by applying perpendicular electric field and hence by modifying electron concentration at both sides as seen in Figure 4c.

The self-consistent potential energy averaged on the planes perpendicular to $z$-axis, $\bar{V}(z)$, is presented in Figure 4d. Within PBC, $\bar{V}(z)$ displays a sawtooth behavior. The form of the potential suggests interesting situations for both sides of graphene. For example, one can monitor the work function on both sides. Side-specific effects induced by perpendicular electric field are pronounced in single-layer honeycomb structures consisting of two or three atomic planes, such as silicene,43,47,48 single-layer transition-metal dichalcogenides,49 and graphene bilayer.

The effect of applied perpendicular electric field on the calculated total energies of oxygen adsorbed at different sites on the NEB path between two adjacent B-sites through the T-site is presented in Figure 5. The difference of total energy $\Delta E$, between oxygen adsorbed at the T-site and B-site, is as large as $\sim 1.2$ eV for $\vec{E} = +2.0$ V/Å. However, when the direction of $\vec{E}$ is reversed, $\Delta E$ decreases and becomes even negative for $\vec{E} = -2.0$ V/Å. This is a dramatic effect and is expected to bear on the reduction/oxidation of graphene surfaces. Since the energy barrier between the B-site and T-site can be modified by the applied electric field, the monitoring of oxygen diffusion at the graphene surface will be possible through applied electric field. We note that the magnitudes of the electric fields of $1-2$ V/Å are high but they are in the range that can be applied at least for short times.50

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**Figure 3.** Variation of binding energy $E_{bo}$, oxygen adatom, and height $h$ from the graphene plane with electric field $\vec{E}$, applied perpendicular to the graphene plane. $\vec{E}$ is taken as positive if it is along $z$-direction (or it is pointing toward oxygen adatom) and vice versa. (Results are obtained from AO calculations using PBC.)

**Figure 4.** (a) Atomic configuration showing a single oxygen atom adsorbed at the B-site of a $(5 \times 5)$ graphene supercell with red and brown spheres indicating oxygen adatom and carbon atoms of graphene, respectively. The $xy$ plane coincides with the atomic plane of bare graphene, and $z$-direction is perpendicular to graphene. (b, c) Difference charge density $\Delta \rho$ for the electric field (b) antiparallel ($\vec{E} < 0$) and (c) parallel ($\vec{E} > 0$) to $z$-direction. Yellow (blue) isosurfaces indicate electron accumulation (depletion) induced by $\vec{E}$ applied in different directions. (d) Self-consistent field potential energy averaged on the planes perpendicular to $z$-axis throughout the supercell, $\bar{V}(z)$, for the cases $\vec{E} = 0$, $\vec{E} < 0$, and $\vec{E} > 0$. (Results are obtained from AO calculations using PBC.)

**Figure 5.** Variation of total energy $E_{T}$ of a single oxygen atom adsorbed to each $(5 \times 5)$ graphene supercell under applied perpendicular electric fields $\vec{E}$ on a NEB path between two adjacent B-sites through the T-site. The total energy at the B-site is set to 0 for all cases. The unit of $\vec{E}$ is volts per angstrom. (Results are obtained from AO calculations using PBC.)
We now resolve the above paradoxical situation, namely, that the equilibrium oxygen graphene distance $h$ increases with increasing $E_p$ as shown in Figure 3 and develop a criterion for the strength of bond between graphene and oxygen adatom. To this end, we consider the system consisting of $(5 \times 5)$ graphene supercells with a single oxygen adatom, which are either charged by $Q$ or under a perpendicular electric field $E$ as shown in Figure 6a. We calculated the optimized total energies of this system while oxygen adatom is pulled along $z$-direction perpendicular to the plane of graphene. For each fixed value $\Delta d$ of oxygen adatom from its equilibrium height $h$, carbon atoms around oxygen adatom are relaxed, while the rest of the atoms are fixed to prevent graphene from displacement. These analyses are continued by varying $\Delta d$ for different values of $Q$ [e per $(5 \times 5)$ cell] and for different values of $E$ perpendicular to the graphene plane.

The variation of the total energies with pulling $\Delta d$ are plotted in Figure 6 panels b and c for different values of $Q$ and $E$, respectively. For the sake of comparison, we also included the pulling curves for $Q = 0$ and $E = 0$. These figures convey interesting features regarding the effects of either charging or applied perpendicular electric field on the strength of the bond between graphene and oxygen adatom: Normally, the energy associated with pulling $E_p = E_p[O + \text{graphene}, Q, E, \Delta d] - E_p[O + \text{graphene}, Q, E, \Delta d = 0]$ increases with increasing $\Delta d$, since the system is strained and pulled upward. Eventually it passes through a maximum value denoted by $E^*_{p}$ and drops suddenly at about $0.8 < \Delta d < 0.9 \, \text{Å}$. Our analysis suggests that $E^*_{p}$ can be taken as a measure for the strength of the bond between oxygen adatom and graphene. We note that $E^*_{p}$, namely, the energy barrier to pull out the adsorbed oxygen adatom from graphene surface, is $\sim 2.60 \, \text{eV}$ for both $Q = 0$ and $E = 0$. This energy is consistent with the binding energy calculated for the bridge site. An interesting feature of the present analysis is that $E^*_{p}$ is strongly dependent on charging and electric field. While $E^*_{p}$ increases with $Q > 0$, it decreases dramatically for $Q < 0$. For example, $E^*_{p} = 1.46 \, \text{eV}$ for $Q = −1.0 \, \text{e/cell}$ (or $−0.02 \, \text{e/carbon atom or } \sigma = −0.12 \, \text{C/m}^2$).

Similarly, $E^*_{p}$ can be as low as $\sim 1.14 \, \text{eV}$ under the perpendicular electric field $E = −2 \, \text{V/Å}$. As shown by inset in Figure 6c, a bistability occurs if oxygen atom moves in the reverse direction and hence approaches to the graphene from $\Delta d > 1.0 \, \text{Å}$. Notably, for $Q < 0$, the $E_p$ curve does not experience a sharp fall passing its maximum value. This is related to the excess charge on oxygen atom. These are important results and demonstrate that it is easier to desorb oxygen adatoms from graphene by negatively charging or by applying perpendicular electric field. Under high local charging and local electric field, which can be attained by the sharp tip of a scanning tunneling microscope or by a gate voltage, the reduction of GOX through the desorption of O adatoms can be achieved.

Since the negative charging or negative perpendicular electric field both weaken the bond between oxygen and graphene and hence lower $E^*_{p}$, we next explore their effects on the bond between graphene and oxygen adatom when they both coexist. Thus the negative $E$ of different magnitudes exerts on a negatively charged system consisting of a single oxygen adatom adsorbed to each $(5 \times 5)$ supercell of graphene. We found that effects the same as in Figure 6b,c are attained by applying relatively lower electric field when the system is negatively charged. In particular, adsorbed oxygen moves high above graphene and becomes weakly bound under the electric field $E = −2.5 \, \text{V/Å}$ if the whole system is charged by $Q = −1.0 \, \text{e/cell}$ (or $\sigma = −0.12 \, \text{C/m}^2$). We note that this value is much smaller than the electric field required for desorption of oxygen from a neutral system. In Figure 6d we schematically show different positions of oxygen adatom (bridge- and top-site) and moved away from graphene for desorption occurring under different values of negative $E$ and negative $Q$.

Figure 6. Variation of the pulling energy $E_p$ of a single oxygen adatom adsorbed to each $(5 \times 5)$ supercell of graphene charged by $Q$ or exerted by $E$ with pulling distance along the $z$-axis, $\Delta d$, from its equilibrium height $h$. (a) Atomic configuration. Red (large) and brown (small) spheres indicate oxygen and carbon atoms, respectively. (b) Variation of $E_p$ with $\Delta d$, along $z$-axis for different charging values $Q$. (c) Variation of $E_p$ with $\Delta d$, along $z$-axis for different applied electric fields $E$. All cases have their own equilibrium heights $h$. The maximum value of the pulling energy for each case is specified by $E^*_{p}$. As shown by inset for the case of $Q = 0$ and $E = 0$, a bistability occurs when oxygen atom approaches graphene from a long distance. (d) Positions of adsorbed oxygen atom under different values of electric field $E$ and/or charging $Q$. Green, red, and blue dots indicate respectively oxygen atom adsorbed to the bridge site, adsorbed to the top site, and desorbed by moving away from graphene plane. (Results are obtained from AO calculations using PBC.)
FORMATION OF OXYGEN MOLECULE

Having examined the binding energy, binding site, and diffusion of single oxygen adatoms and their variation with charging and applied electric field, we next consider the formation of O$_2$, which can be essential in deoxidation. Since single oxygen adatom adsorbed to graphene has negative formation energy, one cannot expect that O$_2$ molecule dissociates into two atomic oxygens, both adsorbed to graphene. However, O$_2$ molecules can dissociate at the edges of vacancy defects or holes and subsequently the constituent atomic oxygens are adsorbed to carbon atoms with lower coordination. In view of the negative formation energy, one normally expects that two oxygen atoms adsorbed individually to graphene can readily form O$_2$ in an exothermic process when two atoms are in close proximity. Therefore, the interaction of two oxygen adatoms on graphene is essential for the formation of O$_2$. In Figure 7a we examined O–O interaction for $Q < 0$ and $\vec{E} = 0$ while one O is at the position identified as p and marked by the arrow as shown by inset, and the other one is diffusing from a distant bridge site identified as a. Initially, the interaction between them is weak, but it develops as one O atom is migrating from a toward p through b, c, and d positions. Here a and c correspond to the bridge sites and b and d to the top sites. Here we consider three situations, which are illustrated by three curves denoted I, II, and III. For curve I, the x- and y-coordinates of all carbon atoms of graphene are kept fixed but their z-coordinates are relaxed as the first O adatom migrates from position a to the second O at position p. While the first O is forced to migrate through the path of the minimum energy barrier by optimizing its height from graphene, the second O is fully relaxed. Overcoming the barrier of $\sim 3.3$ eV corresponding to configuration K, O$_2$ is desorbed at G. Curve I is similar to the curve in Figure 5c of ref 16 calculated by the PW method.

For curve II, only one carbon atom out of 72 in the supercell is fixed to prevent underlying graphene from displacing in the course of forced migration of the first O adatom. A relatively smaller barrier of $\sim 2.3$ eV develops between d and H, and eventually one O adatom is desorbed once H is overcome at L. Apparently curves I and II are associated with high energy barriers for the desorption of O$_2$ or single oxygen atom from GOX. A different migration path is followed for curve III: Once the first O adatom arrived at position d, it is fixed there while the second O adatom at position p is forced to the top site at position e. To attain the final configuration J, an energy barrier of 1.3 eV from position c has to be overcome. After J, two O adatoms form O$_2$ and desorb from graphene. Clearly, this path described by curve III has a much lower barrier than those of configurations K and H. The energy barriers of curves I–III are lowered with negative charging.

Larciprete et al. pointed out a dual path described by inset A in Figure 7b, which allows two O adatoms at the bridge sites to move along C–C bonds toward to adjacent top sites. They calculated the energy barrier to be 1.13 eV using PW method and found that it is in good agreement with temperature-programmed desorption (TPD) data. They observed significant O$_2$ desorption at $\sim 500$ K during the thermal annealing of low oxygen density GOX. Here, we first examine the low-energy-barrier dual path proposed by Larciprete et al. and calculate the energy barrier for $Q < 0$ and $\vec{E} = 0$ using the AO method by relaxing all atoms in the supercell except one carbon atom to hinder the displacement of graphene layer. In Figure 7b we present the energy variation of the dual path corresponding to curve I through A, B, C, and D configurations shown by inset. The energy barrier at B configuration is rather low as compared to K and H configurations in Figure 7a. Overcoming an energy barrier of 0.8 eV, two O adatoms become attached to two adjacent top sites of graphene described as configuration C. The energy barrier calculated by AO method is $\sim 0.3$ eV lower than predicted by Larciprete et al., perhaps due to the different parameters of calculations and different basis set. If one of these O atoms is forced toward the other one, an energy barrier of 0.4 eV develops between C and D. The formation of O$_2$ and desorption is achieved at E when D is overcome. A different path specified as curve II in Figure 7b goes to F from C, where one of the O adatoms of configuration C is raised. This way, the formation of O$_2$ is attained without an energy
barrier after configuration C. The atomic configurations corresponding to various stages are described by insets.

Having discussed two paths with low energy barrier leading to the formation of O₂ from GOX, we next examine how these barriers are affected by external agents such as negative charging and applied electric field. When charged by \( Q = -4 \mu\text{C/supercell} \) (\( \tilde{Q} = -0.332 \text{ C/m}^2 \)), the energy variation of curves I and II is modified as presented by curve III in Figure 7b. Two oxygen adatoms migrating from configuration A toward configuration C encounter a small energy barrier of \( \sim 0.1 \text{ eV} \). This is a really small barrier, which can be further lowered or completely suppressed with increasing excess electrons. The application of the electric field of \( E = -2 \text{ V/Å} \) perpendicular to the plane of graphene induces a similar effect shown by curve IV. While the barrier of 0.8 eV at B is suppressed, a small barrier of \( \sim 0.2 \text{ eV} \) near C appears. The energy barrier in curves III and IV is rather small and explains why GOX can easily be deoxidized under external effects.\(^{20,22}\)

**DISCUSSIONS AND CONCLUSIONS**

In order to understand recent experimental works reporting reduction of GOX by charging or by applying electric field, we investigated the effects of these external agents on single oxygen adatoms on graphene. To separate their possible effects on the reduction process from those of hydroxyl groups, here we consider only the epoxy groups. First, we discussed the limitations and artifacts of methods using plane-wave (PW) and local orbital (AO) basis sets within periodic boundary conditions in treating the systems that are either charged or subjected to perpendicular electric field. While both methods have been successful in treating the atomic and electronic structure of various neutral or positively charged adatom–surface complexes, AO calculations hindering the spurious vacuum charging within PBC are found to be appropriate to treat the systems that are either negatively charged or are exerted by a perpendicular electric field. It appears that an artifact of AO calculations cancels out another artifact of PBC. Our related analyses are believed to be very valuable for future theoretical studies including excess charge and electric field.

Determining that AO calculations can provide the proper treatment of one single graphene layer, which is charged negatively or subjected to a perpendicular electric field, we carried out structure-optimized, self-consistent field calculations under specific constraints and NEB calculations between well-defined initial and final configurations. We found that the strength of the bond between graphene and oxygen adatom is weakened with negative charging and/or with perpendicular electric field applied in the direction opposite to oxygen. With negative perpendicular electric field and negative charging both coexisting in the system, the desorption and hence reduction of GOX can take place much more easily. Despite the negative formation energy, the formation of oxygen molecule from individual oxygen adatoms adsorbed to graphene is hindered by the energy barriers of 0.8–1.3 eV. The calculated energy barriers are significantly lower than the sum of the binding energies of two single oxygen adatoms due to the concerted action. In this respect, we note the possibility of another reaction path with an even lower energy barrier.

In conclusion, we showed that the calculated energy barriers on various reaction paths are dramatically lowered by charging the system with excess electrons or by applying a perpendicular electric field. This explains why the reduction of GOX through desorption of oxygen or O₂ is facilitated as reported by earlier experimental studies. Notably, perpendicular electric field can be used also for side-specific functionalization of single-layered and multilayered nanostructures.

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**Notes**

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